

# Synthesis and crystal structure of $\text{Bi}_{6.4}\text{Pb}_{0.6}\text{P}_2\text{O}_{15.2}$ A new polymorph in the series $\text{Bi}_{6+x}\text{M}_{1-x}\text{P}_2\text{O}_{15+y}$

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## Abstract

$\text{Bi}_{6.4}\text{Pb}_{0.6}\text{P}_2\text{O}_{15.2}$  is a polymorph of structures with the general stoichiometry  $\text{Bi}_{6+x}\text{M}_{1-x}\text{P}_2\text{O}_{15+y}$ . However, unlike previously published structures that consist of layers formed by edge sharing  $\text{OBi}_4$  tetrahedra bridged by  $\text{PO}_4$  and  $\text{TO}_6$  ( $T$  = transition metal) tetrahedra and octahedra the title compound's structure is more complex. It is monoclinic,  $C2$ ,  $a = 19.4698(4)$  Å,  $b = 11.3692(3)$  Å,  $c = 16.3809(5)$  Å,  $\beta = 101.167(1)^\circ$ ,  $Z = 10$ . Single-crystal X-ray diffraction data were refined by least squares on  $F^2$  converging to  $R_1 = 0.0387$ ,  $wR_2 = 0.0836$  for 7023 intensities. The crystal twins by mirror reflection across (001) as the twin plane and twin component 1 equals 0.74(1). Oxygen ions are in tetrahedral coordination to four metal ions and the  $\text{O}(\text{BiPb})_4$  units share corners to form layers that are part of the three-dimensional framework. Eight oxygen ions form a cube around the two crystallographically independent Pb ions. Pb–O bond lengths vary from 2.265(14) to 2.869(14) Å. Pairs of such cubes share an edge to form a  $\text{Pb}_3\text{O}_{20}$  unit. The two oxygen ions from the unshared edges are part of irregular Bi polyhedra. Other oxygen ions of Bi polyhedra are part only of  $\text{O}(\text{BiPb})_4$  units, and some oxygen ions of the polyhedra are also part of  $\text{PO}_4$  tetrahedra. One, two, three and or four  $\text{PO}_4$  moieties are connected to the Bi polyhedra. Bi–O bond lengths  $\leq 3.1$  Å vary from 2.090(12) to 3.07(3) Å. The articulations of Pb cubes, Bi polyhedra and  $\text{PO}_4$  tetrahedra link into the three-dimensional structure.

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## 1. Introduction

Significant oxygen ion conductivity in a high-temperature polymorph of  $\text{Bi}_4\text{V}_2\text{O}_{11}$  [1] has led to intensive investigations of the crystal chemistry and physical properties of compounds synthesized in ternary and quaternary systems Bi–Pb—transition metal—P, V, As—O giving rise to complex phosphates, vanadates and arsenates [2–18]. This search for improved oxygen ion conductors has resulted in important contributions to the understanding of the interrelationship between crystal structure and ion conductivity [16,18]. Many of the structures are related to the high-temperature  $\delta$ - $\text{Bi}_2\text{O}_3$  and  $\text{CaF}_2$  motifs that exhibit ion transport properties. Lee et al. [19] synthesized and investigated the ionic conductivity of  $\text{PbBi}_6\text{M}_2\text{O}_{15}$  ( $M = \text{V}, \text{P}, \text{As}$ ) and solid solutions of

$\text{SrBi}_6\text{V}_2\text{O}_{15}$  but did not determine the crystal structure. We have described the syntheses and crystal structures of a new series of compounds  $\text{Bi}_6\text{TP}_2\text{O}_{15+x}$ ,  $T$  = 1st row transition metals [20–22] and as part of this investigation also grew single crystals of  $\text{Bi}_6\text{PbP}_2\text{O}_{15}$  in anticipation that it might be isostructural with compounds of that series. The X-ray diffraction powder pattern of this phase, however, differed from those in this series but matched the X-ray diffraction powder pattern published by Lee et al. [19]. It became evident that it is a polymorph with a new crystal structure and this determination is reported here.

## 2. Experimental

### 2.1. Synthesis

Nominal  $\text{Bi}_6\text{PbP}_2\text{O}_{15}$  was synthesized by the solid-state reactions of bismuth trioxide ( $\text{Bi}_2\text{O}_3$ ), ammonium dihydrogen

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phosphate ( $\text{NH}_4\text{H}_2\text{PO}_4$ ) and lead oxide ( $\text{PbO}$ ). The reactant mixtures were mixed in the ratio of 3:2:1. Prior to their use,  $\text{Bi}_2\text{O}_3$  was dried in air at  $600^\circ\text{C}$  for 24 h. The mixture was initially heated in air at  $195^\circ\text{C}$  for 5 h to decompose  $\text{NH}_4\text{H}_2\text{PO}_4$  and finally at  $600^\circ\text{C}$  for 12 h at a rate of  $120^\circ\text{C}/\text{h}$ . The intermediate product was then ground and reheated in air at  $800^\circ\text{C}$  for 10 h and cooled to RT at the rate of  $150^\circ\text{C}/\text{h}$ . This product was refired at a higher temperature to ensure the completion of the reaction. The melting point of the sample determined by DTA was  $900 \pm 5^\circ\text{C}$ . Single crystals of nominal  $\text{Bi}_6\text{PbP}_2\text{O}_{15}$  were obtained by melting a small amount of the polycrystalline sample and slow cooling in a gold boat.  $\text{Bi}_6\text{PbP}_2\text{O}_{15}$  melts congruently at  $900 \pm 5$ . The temperature of the polycrystalline sample was then raised to  $925^\circ\text{C}$  using a special temperature regime and the melt was kept for 2 h. The melt was slowly cooled at a rate of  $5^\circ\text{C}/\text{h}$  to  $850^\circ\text{C}$ , and then furnace cooled to room temperature. Examination of the melt under a polarizing binocular microscope revealed the presence of pale yellow–green crystals. A polycrystalline sample was analyzed by inductively coupled plasma (ICP) optical emission spectroscopy yielding the Bi:Pb ratio 6.8:0.2 on the basis of  $P = 2$ .

## 2.2. Crystallography

Single-crystal X-ray diffraction data were obtained using a Nonius  $\kappa$  automated CCD diffractometer equipped with a graphite monochromator with  $\text{MoK}\alpha$  radiation,

Table 1  
Crystal data and structure refinement for  $\text{Bi}_{6.40}\text{Pb}_{0.60}\text{P}_2\text{O}_{15.20}$

Empirical formula	$\text{Bi}_{6.40}\text{Pb}_{0.60}\text{P}_2\text{O}_{15.20}$
Formula weight	1766.93
Temperature (K)	293(2)
Wavelength ( $\text{\AA}$ )	0.71073
Crystal system, space group	C2
Unit cell dimensions ( $\text{\AA}$ )	
<i>a</i>	19.4698(4)
<i>b</i>	11.3692(3)
<i>c</i>	16.3809(5)
$\beta$	$101.1674(11)^\circ$
Volume ( $\text{\AA}^3$ )	3557.35(16)
Z, calculated density (g/cm)	10, 8.25
Absorption coefficient ( $\text{mm}^{-1}$ )	86.24
Crystal size (mm)	$0.08 \times 0.05 \times 0.02$
Crystal color	Yellowish
Theta range for data collection	$1.00\text{--}27.48^\circ$
Limiting indices	$-25 \leq h \leq 25, -14 \leq k \leq 14,$ $-21 \leq l \leq 21$
Reflections collected/unique	7023/7023 [ $R(\text{int}) = 0.0000$ ]
Completeness to theta (%)	99.9
Absorption correction	SADABS
Refinement method	Full-matrix least-squares on $F^2$
Data/restraints/parameters	7023/1/339
Goodness-of-fit on $F^2$	1.046
Final $R$ indices [ $I > 2\sigma(I)$ ]	$R_1 = 0.0387, wR_2 = 0.0836$
$R$ indices (all data)	$R_1 = 0.0387, wR_2 = 0.0836$
Extinction coefficient	0.000146(4)
Largest diff. peak and hole ( $\text{e}\text{\AA}^{-3}$ )	5.492 and $-5.568$

Table 2

Atomic coordinates ( $\times 10^4$ ) and equivalent isotropic displacement parameters ( $\text{\AA}^2 \times 10^3$ ) for  $\text{Bi}_{6.40}\text{Pb}_{0.60}\text{P}_2\text{O}_{15.20}$

Atom	<i>x</i>	<i>y</i>	<i>z</i>	$U(\text{eq})^a$
Bi(1)	10000	121(1)	10000	13(1)
Bi(2)	8818(1)	1664(1)	8033(1)	10(1)
Bi(3)	8371(1)	$-1635(1)$	10035(1)	11(1)
Bi(4)	9398(1)	6346(1)	12049(1)	13(1)
Bi(5)	8921(1)	$-1832(1)$	8096(1)	13(1)
Bi(6)	8400(1)	5080(1)	10283(1)	17(1)
Bi(7)	7330(1)	6656(1)	8261(1)	8(1)
Bi(8)	7197(1)	3373(1)	7919(1)	9(1)
Bi(9)	7698(1)	$-6288(1)$	5984(1)	9(1)
Bi(10)	6244(1)	$-1378(1)$	5932(1)	7(1)
Bi(11)	4486(1)	222(1)	5980(1)	7(1)
Bi(12)	9579(1)	$-1450(1)$	6008(1)	8(1)
Bi(13)	7999(1)	$-3048(1)$	6100(1)	11(1)
Bi(14)	6206(1)	$-4588(1)$	6074(1)	8(1)
Bi(15)	7905(1)	309(1)	5973(1)	8(1)
Bi(16)	10000	3421(1)	10000	20(1)
Bi(17)	10476(1)	3172(1)	7889(1)	13(1)
Pb(1)	10000	6740(1)	10000	21(1)
Pb(2)	8866(1)	4909(1)	8136(1)	15(1)
P(1)	9444(3)	1967(5)	6001(3)	7(1)
P(2)	10498(3)	$-256(5)$	8012(4)	9(1)
P(3)	7172(3)	$-214(5)$	7908(4)	10(1)
P(4)	6199(3)	$-8021(5)$	5854(3)	7(1)
P(5)	6620(2)	6859(5)	10077(3)	9(1)
O(1)	10048(7)	$-1200(13)$	7401(10)	19(3)
O(2)	7788(6)	4910(11)	8542(8)	8(3)
O(3)	9242(6)	4904(11)	9534(9)	12(3)
O(4)	9317(6)	$-5261(11)$	11282(8)	10(3)
O(5)	6125(8)	7609(14)	9456(10)	25(4)
O(6)	7931(6)	220(10)	4666(8)	7(3)
O(7)	9630(6)	$-3270(11)$	8422(8)	8(2)
O(8)	8129(6)	$-3087(12)$	7404(8)	11(3)
O(9)	9224(6)	6900(12)	6419(8)	13(3)
O(10)	6956(6)	854(11)	8369(8)	9(3)
O(11)	6535(8)	$-711(13)$	7293(10)	24(3)
O(12)	7395(9)	$-1142(16)$	8569(12)	37(4)
O(13)	11062(12)	$-980(20)$	8576(17)	73(7)
O(14)	9300(9)	797(15)	5584(11)	32(4)
O(15)	7887(6)	$-401(11)$	3117(8)	11(3)
O(16)	10200(10)	2260(18)	6118(14)	50(5)
O(17)	10032(12)	300(20)	8542(15)	59(6)
O(18)	7774(8)	37(14)	7470(11)	25(4)
O(19)	8949(7)	2897(13)	5469(10)	22(3)
O(20)	6300(8)	5665(14)	10260(11)	27(4)
O(21)	10842(12)	540(20)	7512(15)	58(6)
O(22)	7294(8)	6635(15)	9738(11)	32(4)
O(23)	8234(8)	12570(15)	9101(11)	32(4)
O(24)	9236(13)	1840(20)	6847(17)	82(8)
O(25)	6160(7)	$-6873(13)$	5333(10)	21(3)
O(26)	6750(9)	$-7828(16)$	6640(12)	42(5)
O(27)	5492(9)	$-8352(16)$	6014(12)	40(4)
O(28)	6485(8)	$-9014(15)$	5345(11)	30(4)
O(29)	9327(7)	$-1410(13)$	9607(10)	20(3)
O(30)	9948(6)	4784(11)	7225(8)	9(3)
O(31)	7245(6)	$-1158(11)$	5649(8)	8(3)
O(32)	6692(6)	$-2976(11)$	6418(8)	9(3)
O(33)	8475(6)	$-4984(11)$	6356(9)	10(3)
O(34)	9541(6)	3101(11)	8436(9)	13(3)
O(35)	8602(6)	$-1101(11)$	6369(8)	7(3)
O(36)	8150(6)	3069(11)	7473(9)	11(3)
O(37)	8908(7)	6791(12)	10622(9)	14(3)
O(38)	8330(7)	$-2863(13)$	8972(10)	25(3)

<sup>a</sup> $U(\text{eq})$  is defined as one-third of the trace of the orthogonalized  $U_{ij}$  tensor.

$\lambda = 0.71073 \text{ \AA}$ . The diffracted intensities generated by a scan of  $2.0^\circ \omega$  and 340 s exposure time per frame were recorded on 93 frames at  $\phi = 186^\circ$ , 58 frames over a range of  $116^\circ \omega$ , and 55 frames over a range of  $110^\circ \omega$ . The intensities were collected on the basis of a C-centered monoclinic cell,  $a = 19.4500(3) \text{ \AA}$ ,  $b = 11.3388(2) \text{ \AA}$ ,  $c = 16.3379(3) \text{ \AA}$ ,  $\beta = 101.0773(6)^\circ$ . Data reduction and scaling were performed using DENZO-SMN [23]. Details of crystal data, data collection and structure refinement are

listed in Table 1. The structure was solved with the direct methods program SHELXS [24] in space group  $C2$  that yielded the heavy atom positions. Difference electron density maps revealed the phosphorus and oxygen atoms. The refinement proceeded by least squares using SHELXL [24], DENZO-style merged intensities, anisotropic displacement parameters for Bi and Pb, eventually converging to  $R_1 = 0.0494$  and Flack  $x$  parameter 0.24. The program ROTAX [25] indicated that the crystal was a

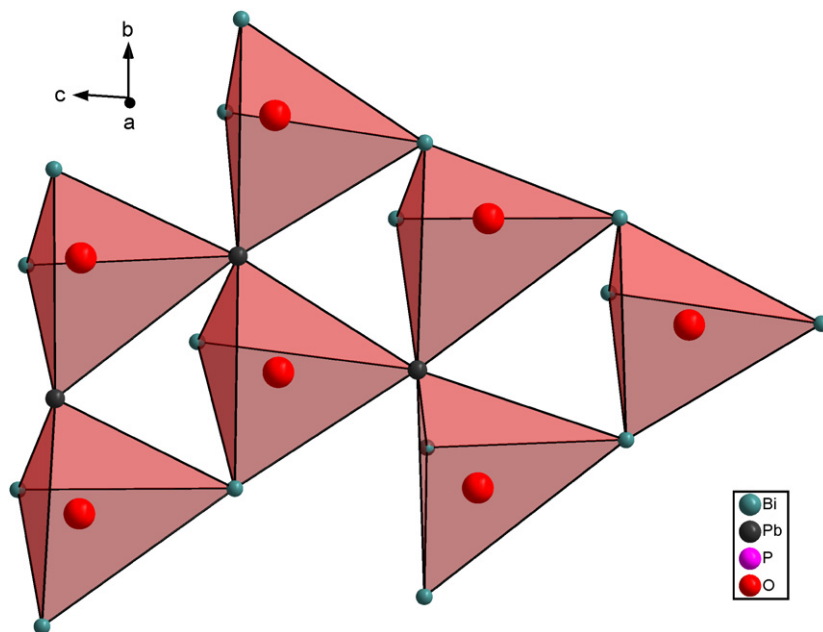


Fig. 1. Section of the crystal structure of  $\text{Bi}_{6.4}\text{Pb}_{0.6}\text{P}_2\text{O}_{15.2}$  showing the corner sharing oxygen tetrahedra  $\text{O}(\text{BiPb})_4$  in the  $b$ - $c$  plane.

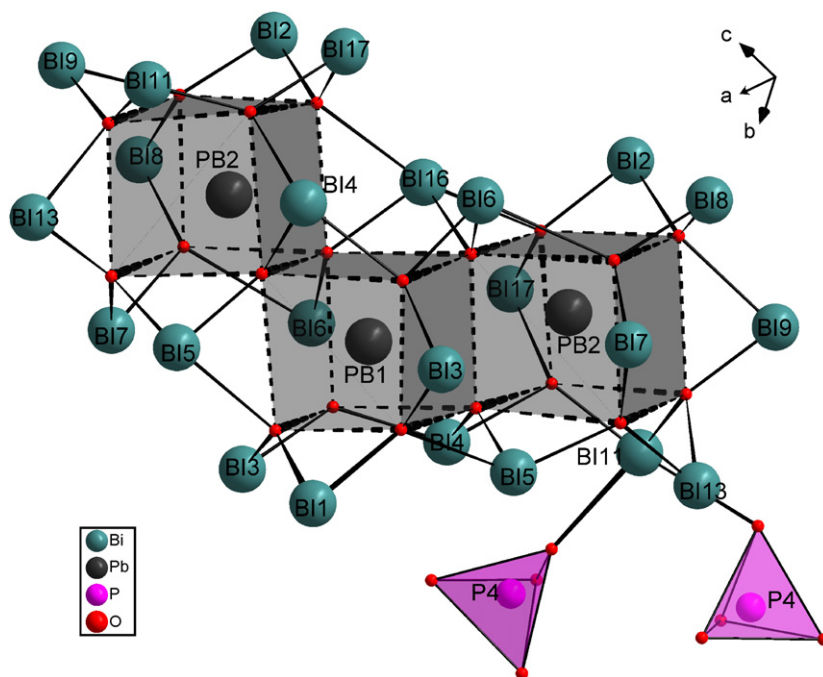


Fig. 2. Section of the crystal structure of  $\text{Bi}_{6.4}\text{Pb}_{0.6}\text{P}_2\text{O}_{15.2}$  showing the articulation of the cubic Pb polyhedra, the bonding of unshared oxygen edges to Bi and illustrating the connection of two  $\text{PO}_4$  tetrahedra to Bi.

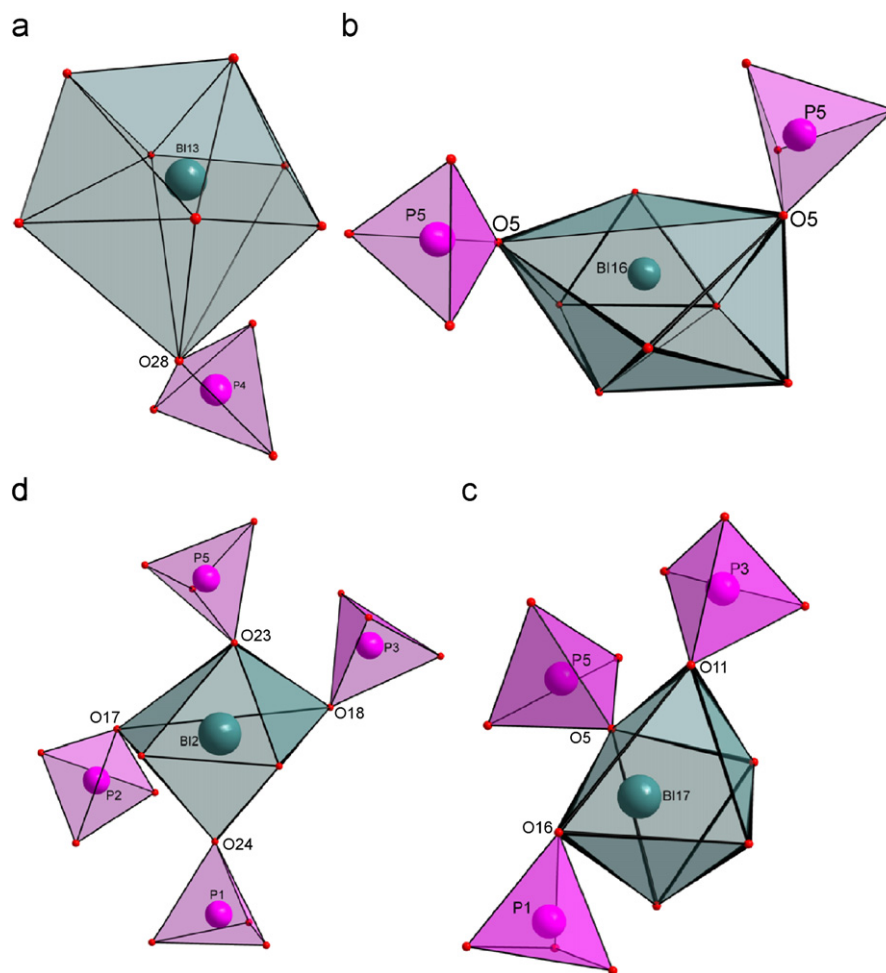


Fig. 3. Selected Bi–O polyhedra and bonding to (a) one, (b) two, (c) three and (d) four PO<sub>4</sub> moieties.

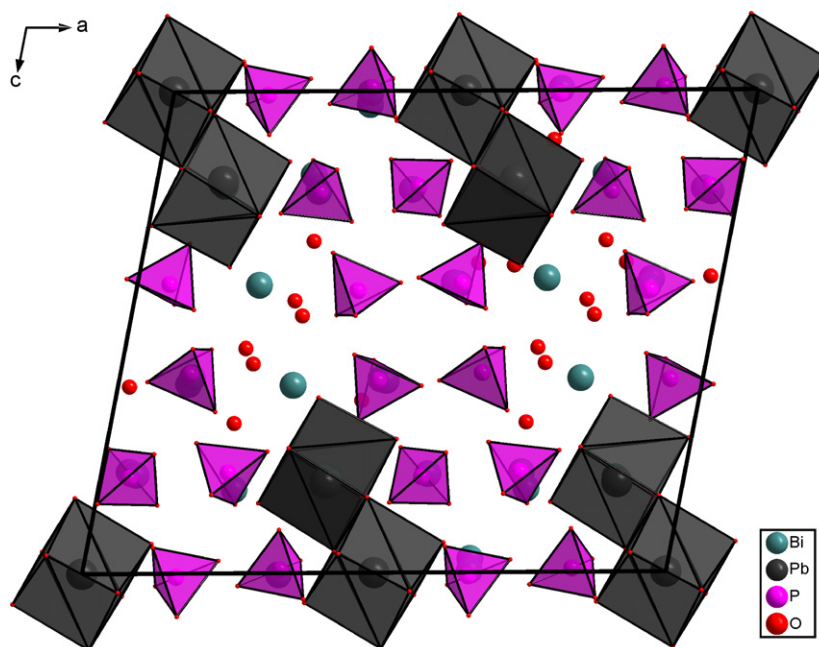


Fig. 4. The crystal structure of Bi<sub>6.4</sub>Pb<sub>0.6</sub>P<sub>2</sub>O<sub>15.2</sub> looking parallel to the *b*-axis. For the sake of clarity only the Pb and P polyhedra are shown. Bonds among Bi and oxygen ions are omitted.

Table 3  
Bond lengths (Å), valence bond sums (VBS) and angles (deg) for Bi<sub>6.4</sub>Pb<sub>0.6</sub>P<sub>2</sub>O<sub>15.2</sub>

Bi(1)–O(29)	2.199(15)	Bi(2)–O(36)	2.151(13)	Bi(3)–O(29)	2.126(13)	Bi(4)–O(4)#5	2.206(13)	Bi(5)–O(7)	2.141(12)
Bi(1)–O(29)#1	2.199(15)	Bi(2)–O(34)	2.175(13)	Bi(3)–O(37)#4	2.198(14)	Bi(4)–O(7)#6	2.220(11)	Bi(5)–O(8)	2.240(13)
Bi(1)–O(17)#1	2.41(2)	Bi(2)–O(24)	2.26(3)	Bi(3)–O(38)	2.220(16)	Bi(4)–O(30)#1	2.366(12)	Bi(5)–O(38)	2.323(15)
Bi(1)–O(17)	2.41(2)	Bi(2)–O(23)#4	2.488(16)	Bi(3)–O(13)#1	2.44(3)	Bi(4)–O(37)	2.402(14)	Bi(5)–O(29)	2.496(16)
Bi(1)–O(20)#2	2.560(15)	Bi(2)–O(18)	2.770(16)	Bi(3)–O(20)#3	2.757(16)	Bi(4)–O(10)#7	2.653(12)	Bi(5)–O(1)	2.756(13)
Bi(1)–O(20)#3	2.560(15)	Bi(2)–O(17)	2.82(2)	Bi(3)–O(12)	2.816(18)	Bi(4)–O(1)#6	3.063(15)	Bi(5)–O(35)	2.897(13)
		Bi(2)–O(20)#3	3.068(16)	Bi(3)–O(22)#4	2.848(16)			Bi(5)–O(18)	3.108(16)
VBS 2.93		VBS 3.02		VBS 3.22		VBS 2.83		VBS 2.90	
Bi(6)–O(37)	2.203(14)	Bi(7)–O(38)#5	2.138(15)	Bi(8)–O(36)	2.150(12)	Bi(9)–O(33)	2.121(13)	Bi(10)–O(32)	2.103(12)
Bi(6)–O(4)#5	2.210(13)	Bi(7)–O(2)	2.189(12)	Bi(8)–O(15)#10	2.178(13)	Bi(9)–O(6)#11	2.251(12)	Bi(10)–O(31)	2.104(11)
Bi(6)–O(3)	2.238(12)	Bi(7)–O(8)#5	2.306(12)	Bi(8)–O(2)	2.229(13)	Bi(9)–O(15)#11	2.266(12)	Bi(10)–O(11)	2.318(16)
Bi(6)–O(10)#7	2.594(13)	Bi(7)–O(22)	2.435(17)	Bi(8)–O(26)#5	2.511(19)	Bi(9)–O(36)#4	2.534(14)	Bi(10)–O(19)#11	2.399(16)
Bi(6)–O(22)	2.796(16)	Bi(7)–O(12)#5	2.552(18)	Bi(8)–O(23)#4	2.672(18)	Bi(9)–O(31)#11	2.703(13)	Bi(10)–O(16)#12	2.62(2)
Bi(6)–O(2)	2.876(14)	Bi(7)–O(32)#5	3.063(13)	Bi(8)–O(13)#9	2.74(2)	Bi(9)–O(19)#4	2.881(14)	Bi(10)–O(28)#5	2.923(16)
Bi(6)–O(5)#3	2.962(15)			Bi(8)–O(10)	3.016(12)	Bi(9)–O(26)	2.898(18)		
Bi(6)–O(12)#7	2.999(17)					Bi(9)–O(25)	3.052(14)		
VBS 2.95		VBS 3.09		VBS 3.14		VBS 3.02		VBS 3.28	
Bi(11)–O(30)#12	2.123(13)	Bi(12)–O(35)	2.135(11)	Bi(13)–O(8)	2.102(13)	Bi(14)–O(32)	2.090(12)	Bi(15)–O(31)	2.109(12)
Bi(11)–O(9)#12	2.136(13)	Bi(12)–O(9)#4	2.152(13)	Bi(13)–O(9)#4	2.342(12)	Bi(14)–O(15)#11	2.198(13)	Bi(15)–O(35)	2.120(12)
Bi(11)–O(33)#9	2.186(12)	Bi(12)–O(1)	2.305(16)	Bi(13)–O(33)	2.393(13)	Bi(14)–O(6)#11	2.265(12)	Bi(15)–O(6)	2.155(13)
Bi(11)–O(27)#5	2.536(18)	Bi(12)–O(25)#10	2.430(16)	Bi(13)–O(35)	2.505(12)	Bi(14)–O(21)#12	2.59(2)	Bi(15)–O(18)	2.532(16)
Bi(11)–O(28)#14	2.729(17)	Bi(12)–O(14)	2.675(17)	Bi(13)–O(31)	2.627(12)	Bi(14)–O(14)#11	2.737(18)	Bi(15)–O(28)#5	2.861(16)
Bi(11)–O(19)#12	2.905(15)	Bi(12)–O(27)#15	2.799(17)	Bi(13)–O(32)	2.695(12)	Bi(14)–O(25)	2.862(15)	Bi(15)–O(14)	2.961(16)
				Bi(13)–O(6)#11	2.802(12)	Bi(14)–O(16)#12	2.88(2)		
				Bi(13)–O(28)#10	2.956(16)				
VBS 3.19		VBS 3.10		VBS 2.98		VBS 3.08		VBS 3.34	
Bi(16)–O(3)#1	2.273(13)	Bi(17)–O(34)	2.181(12)	Pb(1)–O(29)#6	2.496(15)	Pb(2)–O(3)	2.265(14)		
Bi(16)–O(3)	2.273(13)	Bi(17)–O(4)#6	2.229(13)	Pb(1)–O(29)#5	2.496(15)	Pb(2)–O(2)	2.321(11)		
Bi(16)–O(34)	2.571(15)	Bi(17)–O(30)	2.273(13)	Pb(1)–O(37)#1	2.530(13)	Pb(2)–O(34)	2.437(13)		
Bi(16)–O(34)#1	2.571(15)	Bi(17)–O(5)#2	2.708(17)	Pb(1)–O(37)	2.530(13)	Pb(2)–O(7)#5	2.540(12)		
Bi(16)–O(5)#2	2.683(15)	Bi(17)–O(11)#15	2.757(14)	Pb(1)–O(7)#5	2.545(13)	Pb(2)–O(36)	2.630(13)		
Bi(16)–O(5)#3	2.683(15)	Bi(17)–O(16)	3.03(2)	Pb(1)–O(7)#6	2.545(13)	Pb(2)–O(30)	2.810(11)		
Bi(16)–O(4)#6	3.083(12)	Bi(17)–O(24)	3.07(3)	Pb(1)–O(3)	2.585(13)	Pb(2)–O(8)#5	2.832(13)		
Bi(16)–O(4)#5	3.083(12)			Pb(1)–O(3)#1	2.585(13)	Pb(2)–O(33)#5	2.869(14)		
VBS 2.33		VBS 2.67		VBS 2.59		VBS 2.74			
P(1)–O(16)	1.48(2)	P(2)–O(21)	1.47(2)	P(3)–O(12)	1.514(19)	P(4)–O(27)	1.497(17)	P(5)–O(5)	1.521(17)
P(1)–O(14)	1.497(18)	P(2)–O(17)	1.51(2)	P(3)–O(18)	1.515(15)	P(4)–O(26)	1.52(2)	P(5)–O(22)	1.541(16)
P(1)–O(24)	1.52(3)	P(2)–O(13)	1.53(3)	P(3)–O(10)	1.532(13)	P(4)–O(25)	1.552(16)	P(5)–O(20)	1.547(17)
P(1)–O(19)	1.576(16)	P(2)–O(1)	1.607(16)	P(3)–O(11)	1.545(16)	P(4)–O(28)	1.569(17)	P(5)–O(23)#3	1.549(19)
O(16)–P(1)–O(14)	110.6(11)	O(21)–P(2)–O(17)	116.9(13)	O(12)–P(3)–O(18)	109.2(9)	O(27)–P(4)–O(26)	114.1(10)	O(5)–P(5)–O(22)	109.0(9)
O(16)–P(1)–O(24)	109.6(13)	O(21)–P(2)–O(13)	108.6(13)	O(12)–P(3)–O(10)	105.5(9)	O(27)–P(4)–O(25)	111.1(9)	O(5)–P(5)–O(20)	113.2(9)
O(14)–P(1)–O(24)	105.7(13)	O(17)–P(2)–O(13)	108.5(14)	O(18)–P(3)–O(10)	113.3(8)	O(26)–P(4)–O(25)	107.1(10)	O(22)–P(5)–O(20)	109.1(9)
O(16)–P(1)–O(19)	113.9(10)	O(21)–P(2)–O(1)	108.6(11)	O(12)–P(3)–O(11)	107.1(9)	O(27)–P(4)–O(28)	110.2(10)	O(5)–P(5)–O(23)#3	106.0(10)
O(14)–P(1)–O(19)	107.6(10)	O(17)–P(2)–O(1)	108.7(11)	O(18)–P(3)–O(11)	111.0(9)	O(26)–P(4)–O(28)	106.7(10)	O(22)–P(5)–O(23)#3	112.0(9)
O(24)–P(1)–O(19)	108.9(12)	O(13)–P(2)–O(1)	104.9(12)	O(10)–P(3)–O(11)	110.4(8)	O(25)–P(4)–O(28)	107.3(8)	O(20)–P(5)–O(23)#3	107.6(9)

Symmetry transformations used to generate equivalent atoms: #1:  $-x+2, y, -z+2$ ; #2:  $x+1/2, y-1/2, z$ ; #3:  $-x+3/2, y-1/2, -z+2$ ; #4:  $x, y-1, z$ ; #5:  $x, y+1, z$ ; #6:  $-x+2, y+1, -z+2$ ; #7:  $-x+3/2, y+1/2, -z+2$ ; #8:  $-x+3/2, y+3/2, -z+2$ ; #9:  $x-1/2, y+1/2, z$ ; #10:  $-x+3/2, y+1/2, -z+1$ ; #11:  $-x+3/2, y-1/2, -z+1$ ; #12:  $x-1/2, y-1/2, z$ ; #13:  $-x+1, y, -z+1$ ; #14:  $-x+1, y+1, -z+1$ ; #15:  $x+1/2, y+1/2, z$ ; #16:  $-x+2, y-1, -z+2$ ; #17:  $-x+3/2, y-3/2, -z+2$ ; #18:  $x+1/2, y+3/2, z$ ; #19:  $-x+3/2, y+3/2, -z+1$ ; #20:  $-x+2, y, -z+1$ ; #21:  $-x+3/2, y-3/2, -z+1$ ; #22:  $x-1/2, y-3/2, z$ ; #23:  $-x+1, y-1, -z+1$ .

twin with (00 1) as the twin plane having a twin component 1 equal to 0.74(1). Including twinning in the refinement yielded  $R_1 = 0.0488$ . The resultant stoichiometry was Bi<sub>6.4</sub>Pb<sub>0.6</sub>P<sub>2</sub>O<sub>15.2</sub>. The ICP derived data were high in Bi content even though the X-ray diffraction powder pattern appeared to be single phase. Absorption corrected intensities using the program SADABS [26] with the same refinement conditions converged to  $R_1 = 0.0387$ . The final atomic parameters are shown in Table 2. Since X-ray

scattering cannot distinguish between Pb and Bi, valence bond sum calculations [27] and crystal chemical considerations were used for the atom assignment.

### 3. Results and discussion

The crystal architecture is complex and is best described by selected fragments. The motif is consistent with that of previously published structures. Oxygen ions are in



tetrahedral coordination to four metal ions and the O(BiPb)<sub>4</sub> units share corners to form part of the three-dimensional framework (Fig. 1). Pb1 and Pb2 ions are in cubic coordination to oxygen and share one edge to form a trimer Pb<sub>3</sub>O<sub>20</sub>. The two oxygen ions from the unshared edges are part of Bi polyhedra (Fig. 2). Some of the oxygen ions of Bi polyhedra are also part of PO<sub>4</sub> tetrahedra while other oxygen ions of Bi polyhedra are part only of O(BiPb)<sub>4</sub> units. Selected Bi–O polyhedra and their bonding to one, two, three and four PO<sub>4</sub> moieties are shown in Fig. 3. The articulations of Pb cubes, Bi polyhedra and PO<sub>4</sub> tetrahedra link into the three-dimensional structure as shown in Fig. 4.

In Table 3 are listed bond lengths and valence bond sums for Bi–O, Pb–O and pertinent parameters for the PO<sub>4</sub> tetrahedra. As expected the coordination polyhedra around Bi are distorted due to the presence of the non-binding 6s<sup>2</sup> electrons. The polyhedra vary from distorted octahedra, Bi1, Bi2, Bi4, Bi10 and Bi12 to monocapped, bicapped and tricapped octahedra Bi5, Bi8, Bi9, Bi14, Bi15 and Bi17, capped rectangular pyramids Bi6, Bi11, monocapped distorted trigonal prism Bi3, monocapped pentagonal prism Bi13 and a distorted square antiprism Bi16. The polyhedral description around Bi is somewhat arbitrary because of the irregular arrangements of oxygen forced by the presence of the 6s<sup>2</sup> electrons and the cut off of bonds at  $\leq 3.11 \text{ \AA}$ . The articulations of these tetrahedra and polyhedra are shown in Fig. 4 and provide rigidity to the three-dimensional framework.

#### 4. Conclusion

The relatively low reported conductivities of 10<sup>-5</sup> to 10<sup>-7</sup> S/cm at 500 °C for these materials [19] can be ascribed to the rigid structure formed by the articulation of cubic, tetrahedral and irregular polyhedra. The introduction of defects, e.g. vacancies and aliovalent substitutions improve anion transport [16,18].

#### Supplementary materials

The crystallographic cif file for Bi<sub>6.4</sub>Pb<sub>0.6</sub>P<sub>2</sub>O<sub>15.2</sub> was deposited with FIZ Karlsruhe as CSD number 418094. The data may be obtained without charge from FIZ Karlsruhe; fax: +49 7247 808 666; or e-mail: crysdata@fiz-karlsruhe.de.

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